

		Mark	Comment	Sub
1(i)	$6 \text{ m s}^{-1}$ $4 \text{ m s}^{-2}$	B1 B1	Neglect units. Neglect units.	2
(ii)	$v(5) = 6 + 4 \times 5 = 26$ $s(5) = 6 \times 5 + 0.5 \times 4 \times 25 = 80$ so 80 m	B1 M1 A1	Or equiv. FT (i) and <b>their</b> $v(5)$ where necessary. cao	3
(iii)	distance is 80 + $26 \times (15 - 5) + 0.5 \times 3 \times (15 - 5)^2$ = 490 m	M1 M1 A1	Their 80 + attempt at distance with $a = 3$ Appropria <i>uvast</i> . Allow $t = 15$ . FT <b>their</b> $v(5)$ . cao	3
		<b>8</b>		

		Mark	Comment	
2	$a = 12 - 6t$ $a = 0$ gives $t = 2$ $x = \int (2 + 12t - 3t^2) dx$ $2t + 6t^2 - t^3 + C$ $x = 3$ when $t = 0$ so $3 = C$ and $x = 2t + 6t^2 - t^3 + 3$ $x(2) = 4 + 24 - 8 + 3 = 23 \text{ m}$	M1 A1 F1  M1 A1  M1  A1  B1	Differentiation, at least one term correct. Follow <b>their</b> $a$ Integration indefinite or definite, at least one term correct. Correct. Need not be simplified. Allow as definite integral. Ignore $C$ or limits Allow $x = \pm 3$ or argue it is $\int_0^2$ from A then $\pm 3$ Award if seen WWW or $x = 2t + 6t^2 - t^3$ seen with +3 added later. FT <b>their</b> $t$ and <b>their</b> $x$ if obtained by integration but not if -3 obtained instead of +3. [If 20 m seen WWW for displacement award SC6] [Award SC1 for position if constant acceleration used for displacement and then +3 applied]	8
		8		

		mark		sub
3	$(v =)12 - 3t^2$ $v = 0 \Rightarrow 12 - 3t^2 = 0$ so $t^2 = 4$ and $t = \pm 2$ $x = \pm 16$	M1 A1 M1 A1 A1	Differentiating Allow confusion of notation, including $x =$ Dep on 1 <sup>st</sup> M1. Equating to zero. Accept one answer only but no extra answers. FT only if quadratic or higher degree. cao. Must have both and no extra answers.	
				5

4		mark	notes
(i)			
(A)	4 m	B1	
(B)	$12 - (-4) = 16$ m	M1 A1	Looking for distance. Need evidence of taking account of +ve and -ve displacements.
(C)	$1 < t < 3.5$	B1 B1	The values 1 and 3.5 Strict inequality
(D)	$t = 1, t = 3.5$	B1 6	Do not award if extra values given.
(ii)	$v = -8t + 8$  $a = -8$	M1 A1 F1 3	Differentiating
(iii)	$8t + 8 = 4$ so $t = 0.5$ so 0.5 s  $-8t + 8 = -4$ so $t = 1.5$ so 1.5 s	B1  B1 2	FT <b>their</b> $v$ .  FT <b>their</b> $v$ .
(iv)	<p><b>method 1</b> Need velocity at <math>t = 3</math> <math>v(3) = -8 \times 3 + 8 = -16</math> <b>either</b> <math>v = \int 32 dt = 32t + C</math> <math>v = -16</math> when <math>t = 3</math> gives <math>v = 32t - 112</math> <math>y = \int (32t - 112) dt = 16t^2 - 112t + D</math>  <math>y = 0</math> when <math>t = 3</math> gives <math>y = 16t^2 - 112t + 192</math> <b>or</b> <math>y = -16 \times (t - 3) + \frac{1}{2} \times 32 \times (t - 3)^2</math></p> <p>(so <math>y = 16t^2 - 112t + 192</math>)</p> <p><b>method 2</b> Since accn is constant, the displacement <math>y</math> is a quadratic function. Since we have <math>y = 0</math> at <math>t = 3</math> and <math>t = 4</math> <math>y = k(t - 3)(t - 4)</math>  When <math>t = 3.5, y = -4</math> so <math>-4 = k \times \frac{1}{2} \times -\frac{1}{2}</math> so <math>k = 16</math> (and <math>y = 16t^2 - 112t + 192</math>)</p>	B1  M1 A1 M1  A1  M1 A1 M1 A1  M1 A1 B1  M1 A1	<p>FT <b>their</b> <math>v</math> from (ii)</p> <p>Accept <math>32t + C</math> or <math>32t</math>. SC1 if <math>\int_3^4 32 dt</math> attempted.</p> <p>Use of <b>their</b> -16 from an attempt at <math>v</math> when <math>t=3</math></p> <p>FT <b>their</b> <math>v</math> of the form <math>pt + q</math> with <math>p \neq 0</math> and <math>q \neq 0</math>. Accept if at least 1 term correct. Accept no <math>D</math>.</p> <p>cao</p> <p>Use of <math>s = ut + \frac{1}{2}at^2</math></p> <p>Use of <b>their</b> -16 (not 0) from an attempt at <math>v</math> when <math>t=3</math> and 32. Condone use of just <math>t</math></p> <p>Use of <math>t \pm 3</math></p> <p>cao</p> <p>Use of a quadratic function (condone no <math>k</math>) Correct use of roots <math>k</math> present</p> <p>Or consider velocity at <math>t = 3</math> cao Accept <math>k</math> without <math>y</math> simplified.</p>
PhysicsAndMathsTutor.com		16	

	mark	comment	sub
<b>5(i)</b> The line is not straight	B1	Any valid comment	1
<b>(ii)</b> $a = 3 - \frac{6t}{8}$  $a(4) = 0$ The sprinter has reached a steady speed	M1  F1 E1	Attempt to differentiate. Accept 1 term correct but not $3 - \frac{3t}{8}$ .  Accept 'stopped accelerating' but not just $a = 0$ . Do not FT $a(4) \neq 0$ .	3
<b>(iii)</b> We require $\int_1^4 \left( 3t - \frac{3t^2}{8} \right) dt$  $= \left[ \frac{3t^2}{2} - \frac{t^3}{8} \right]_1^4$  $= (24 - 8) - \left( \frac{3}{2} - \frac{1}{8} \right)$  $= 14\frac{5}{8} \text{ m (14.625 m)}$	M1  A1  M1  A1	Integrating. Neglect limits.  One term correct. Neglect limits.  Correct limits subst in integral. Subtraction seen. If arb constant used, evaluated to give $s = 0$ when $t = 1$ and then sub $t = 4$ . cao. Any form. [If trapezium rule used M1 use of rule (must be clear method and at least two regions) A1 correctly applied M1 At least 6 regions used A1 Answer correct to at least 2 s.f.	4
8			

<b>6</b>				
(i)	$8 \text{ m s}^{-1}$ (in the negative direction)	B1	Allow $\pm$ and no direction indicated	1
(ii)	$(t+2)(t-4) = 0$ so $t = -2$ or $4$	M1 A1	Equating $v$ to zero and solving or subst If subst used then both must be clearly shown	2
(iii)	$a = 2t - 2$  $a = 0$ when $t = 1$ $v(1) = 1 - 2 - 8 = -9$ so $9 \text{ m s}^{-1}$ in the negative direction  (1, -9)	M1 A1 F1  A1  B1	Differentiating Correct  Accept $-9$ but not $9$ without comment  FT	5
(iv)	$\int_1^4 (t^2 - 2t - 8) \, dx$  $= \left[ \frac{t^3}{3} - t^2 - 8t \right]_1^4$  $= \left( \frac{64}{3} - 16 - 32 \right) - \left( \frac{1}{3} - 1 - 8 \right)$  $= -18$  distance is $18 \text{ m}$	M1  A1  M1  A1  A1	Attempt at integration. Ignore limits.  Correct integration. Ignore limits.  Attempt to sub correct limits and subtract  Limits correctly evaluated. Award if $-18$ seen but no need to evaluate Award even if $-18$ not seen. Do not award for $-18$ . cao	5
(v)	$2 \times 18 = 36 \text{ m}$	F1	Award for $2 \times$ <b>their</b> (iv).	1
(vi)	$\int_4^5 (t^2 - 2t - 8) \, dx = \left[ \frac{t^3}{3} - t^2 - 8t \right]_4^5$  $= \left( \frac{125}{3} - 25 - 40 \right) - \left( -\frac{80}{3} \right) = 3\frac{1}{3}$  so $3\frac{1}{3} + 18 = 21\frac{1}{3} \text{ m}$	M1  A1  A1	$\int_4^5$ attempted or, otherwise, complete method seen.  Correct substitution  Award for $3\frac{1}{3} +$ <b>their</b> (positive) (iv)	3
				17